Well-formedness

Formalization of all context conditions (*static semantics*) "Type system++"

When do we have enough?

If nothing bad can happen during the execution of well-formed programs

How is "nothing bad can happen" formalized? Execution does not get stuck (*type safety*, later)

Overview

- Definite assignment
- Method overriding
- Well-formedness

Definite assignment

Definite assignment

Variables must be assigned to before use

Fields are automatically initialized with their default value upon object creation

In theory

Thm It is in general undecidable if ^a variable/field has been initialized before use.

Proof if (b) V := Val ^v else unit; Var V

- 1. V is initialized before use iff b does not evaluate to false.
- 2. Therefore ^a program analyzer would need to decide whether *b* can evaluate to false.
- 3. This is undecidable for arbitrary *b*. Take "Turing machine k with input k terminates with output 0" (realized in Jinja as ^a search procedure). There is no program that can decide this for every $k.$

Fact It is easy to check if ^a variable has been initialized before use: if in doubt, be conservative.

Examples:

- if (b) $V :=$ Val v; Var V is rejected because \bm{b} could be false. What if *b* is never false? Then *if* is pointless!
- if (\bm{b}_1) V $:=$ Val v $_1;$ if (\bm{b}_2) V $:=$ Val v $_2;$ Var V is rejected because \bm{b}_1 and \bm{b}_2 could be false.

Rejection is not ^a problem:

Insert dummy initialization $V := ValV$ right after declaration of V.

Fact It is hard to check if ^a field of an object has been initialized before use.

Example: Let p be a formal parameter of class type. Inside the method body

- variable ρ is initialized,
- but is field F of p initialized??

Therefore Java and Jinja initialize all fields of an object with their default value.

Function A **(1)**

 \mathcal{A} :: expr \Rightarrow vname set

 $A e =$ the set of all (global) variables that are necessarily assigned to if e terminates normally

```
\mathcal{A} (new \mathbf{C}) = {}
A (Cast C e) = A e
\mathcal{A} (Val v) = {}
A (e<sub>1</sub> «bop» e<sub>2</sub>) = A e<sub>1</sub> \cup A e<sub>2</sub>
\mathcal{A} (Var V) = {}
\mathcal{A} (V := e) = {V} ∪ \mathcal{A} e
A(e.F\{D\}) = A e\mathcal{A} (e<sub>1</sub>.F{D} := e<sub>2</sub>) = \mathcal{A} e<sub>1</sub> \cup A e<sub>2</sub>
A(\mathbf{e}.M(\mathbf{e}s)) = A \mathbf{e} \cup (\bigcup_{e \in set \mathbf{e}s} A \mathbf{e})
```
Function A **(2)**

 $A \{V: T: e\}$ = $A e - \{V\}$ $A(\mathbf{e}_1; \mathbf{e}_2) = A \mathbf{e}_1 \cup A \mathbf{e}_2$ A (if (e) e_1 else e_2) = $A e \cup (A e_1 \cap A e_2)$ $A (while (b) e) = A b$ $A (throw e) = {V | True}$ A (try e_1 catch(C V) e_2) = A $e_1 \cap (A \cdot e_2 - \{V\})$

Motivation for *throw*:

A (if (e) $V :=$ Val v else throw e_2) = {V}

Function D **(1)**

 $\mathcal{D} \;::\; \mathsf{expr} \Rightarrow \mathsf{vname}\; \mathsf{set} \Rightarrow \mathsf{bool}$

 $\mathcal D$ e A =

if initially all variables in A are initialized

then execution of e does not access an uninitialized variable

$$
D (new C) A = True
$$

\n
$$
D (Cast C e) A = D e A
$$

\n
$$
D (Val V) A = True
$$

\n
$$
D (e_1 \text{ «bop» } e_2) A = (D e_1 A \land D e_2 (A \cup A e_1))
$$

\n
$$
D (Var V) A = (V \in A)
$$

\n
$$
D (V := e) A = D e A
$$

\n
$$
D (e \cdot F\{D\}) A = D e A
$$

\n
$$
D (e_1 \cdot F\{D\}) = e_2) A = (D e_1 A \land D e_2 (A \cup A e_1))
$$

Function D **(2)**

 $\mathcal{D}\ \{\mathsf{V}\text{:}\mathsf{T};\,\mathsf{e}\}\ A=\mathcal{D}\ \mathsf{e}\ (\mathsf{A}-\{\mathsf{V}\})$ $\mathcal{D} \, \left(\bm{e}_1 \, \mathit{\cdot} \, \; \bm{e}_2 \right) \, \bm{A} = \left(\mathcal{D} \, \, \bm{e}_1 \, \, \bm{A} \wedge \mathcal{D} \, \, \bm{e}_2 \, \left(\bm{A} \cup \mathcal{A} \, \, \bm{e}_1 \right) \right)$ $\mathcal{D} \ (\texttt{if} \ (\boldsymbol e) \ \boldsymbol e_1 \ \texttt{else} \ \boldsymbol e_2) \ \boldsymbol A =$ $(D \in A \wedge D \in A (A \cup A \in A) \wedge D \in A (A \cup A \in A))$ $\mathcal D$ (while $(\bm b)$ $\bm e)$ $\bm A = (\mathcal D ~\bm b ~\bm A ~\wedge~ \mathcal D ~\bm e ~(\bm A \cup \mathcal A ~\bm b))$ $\mathcal D$ (throw $\boldsymbol e)$ $\boldsymbol A = \mathcal D$ $\boldsymbol e$ $\boldsymbol A$ \mathcal{D} (try \boldsymbol{e}_1 catch $(\boldsymbol{C} \ \boldsymbol{V}) \ \boldsymbol{e}_2) \ \boldsymbol{A} = (\mathcal{D} \ \boldsymbol{e}_1 \ \boldsymbol{A} \wedge \mathcal{D} \ \boldsymbol{e}_2 \ (\boldsymbol{A} \cup \{ \boldsymbol{V}\}))$

Each method body $(\mathcal{V}\mathbf{s},\mathbf{e})$ must fulfill the condition \mathcal{D} e $(\{ \textit{this} \} \cup \textit{set Vs})$

Thm If $P \vdash \langle {\bm e},({\bm h},I)\rangle \Rightarrow \langle {\bm e}^{\prime},({\bm h}^{\prime},I^{\prime})\rangle$ then ${\cal A} \hspace{0.1cm} {\bm e} \hspace{0.1cm} \subseteq {\bm d}$ om l' **Proof** by rule induction over ⇒

Correctness of \mathcal{D} : part of type safety proof (later)

Let
$$
e = \text{if } (\text{Var } B) \{V: T; \text{ throw } \}\text{ else } V := \text{true}
$$

\n $A \{V: T; \text{ throw } \}\text{ = } A \text{ (throw } \text{)} - \{V\}$
\n $A e = A(\text{Var } B) \cup (A \{V: T; \text{ throw } \text{]} \cap A(V := \text{true})\text{)}$
\n $= \{\}$
\n $D(e; V := \text{Var } V) \{B\} =$

$$
D(e, v := va(v) \setminus Df -
$$

(D e {B} \wedge D(V := Var V) ({B} \cup \{\})) =
(D e {B} \wedge D(Var V) {B}) =
(D e {B} \wedge V \in {B}) = False

 $A e = \{\}$ is too pessimistic but not incorrect

 \mathcal{A} { $V: T$; throw $_\}$ should be $\set{\mathsf{V} \mid \mathit{True}}$ and not $\set{\mathsf{V} \mid \mathit{True}} - \set{\mathsf{V}}.$

Posible solutions:

- Redefine $\mathcal A$ and $\mathcal D$. Complicated. See Jinja paper.
- Do not allow nested declaration of the same V. Java! Then it does not matter if $\mathsf{V}\in\mathcal{A}$ $\{\mathsf{V}\colon\!mathsf{T};_\}$ or not.

For this course: we leave things as they are and put up with the small imprecision.

Method overriding

The situation

```
class C extends B
\{ \ldotsmethod M(p:T):R = ...
 ...
}
class D extends C
\{ \ldots \}method M(p:T'):R' = ...
 . .
}
```
м in ɒ *overrides* (overwrites, redefines) м in с

How should $\footnotesize{\texttt{T}}$ and $\footnotesize{\texttt{T}}$ ' be related? How should R and R ' be related?

Guiding principle: Type Safety

If e is statically (at compile time) of class C then the evaluation of ^e should yield ^a subclass of C

Then $\bm{e}.\bm{M}(\dots)$ can never fail at runtime as in SmallTalk: Method not understood

Covariance in the result type

$$
R^{\,\prime}\,\leq R
$$

New result type must be *subtype* of old result type

Otherwise:

```
class R' { }
class R extends R' \{ method M2() = \ldots\}\{V:C; V := new D; V.M(...).M2() \}
```
is type correct but semantics gets stuck.

 $\texttt{T} \leq \texttt{T}$ '

New argument type must be *supertype* of old argument type

Why?

- 1. Assume $\texttt{e.M(e')}$ is statically well-typed.
- 2. Assume e has static type ^C.
- 3. Then the static type of $\mathsf{e}^{\;\prime}$ is \leq $\mathbb{T}.$
- 4. Now assume the dynamic type of ^e is ^D
- 5. Thus the dynamic type of e $^{\prime}$ must be \leq T $^{\prime}$.
- 6. But we can only guarantee $\rm e$ $^\prime$ has type \rm_T .

 $7. \implies \texttt{T} \leq \texttt{T}$ '

Example

```
class C extends B
\{ method M(p:T):R = ... \}class D extends C
\{ method M(p:T') : R = p.M2() \}class T { }
class T' extends T \{ method M2():R = \ldots \}Problem?\{V:C; V := new D; V.M(new T)\}\
```
is type correct but semantics gets stuck.

For total functions:

$$
\frac{T \subseteq T' \quad R' \subseteq R}{T' \to R' \subseteq T \to R}
$$

Terminology

Alternatively: antimonotone, monotone

Jinja Contravariant in parameters, covariant in result

Java Invariant:

If $\texttt{T=T}$ $^{\prime}$ then R=R $^{\prime}$ else overloading, not overriding.

Overloading: multiple methods with the same name but different parameter types are visible at the same time. Use static type of actual parameters in method selection (tricky).

Eiffel Covariant in parameters and result (not type safe)

An example

```
class Point
{field x: Integer
 method eq(p:Point):Boolean = (this.x = p.x)
}
class ColPoint extends Point
{field col: Integer
 method eq(cp:ColPoint):Boolean =
```

```
(if (this.x = cp.x) (this.col = cp.col)
 else false)
```
}

```
{p1:color} i p1 := new ColPointp1.x := 5; p1.col := 0;{p2:Point: p2 := new ColPoint; }p2.x := 5; p2.col := 1;p1.eq(p2)}}
```
evaluates to

- in Java: true
- in Eiffel: false
- in Jinja: eq in ColPoint not wellformed!

How can we program ColPoint in Jinja?

```
class ColPoint extends Point
{field col: Integer
 method eqCP(cp:ColPoint):Boolean =
  (if (this.x = cp.x) (this.col = cp.col)
   else false)
}
```
Similar to Java: make argument type part of method name. In Java this happens implicitly via overloading.

Well-formedness

Well-formed program P

wf-J-prog P

- The system classes are declared: {Object, NullPointer, ClassCast, OutOfMemory} \subset set(map fst P)
- No class is declared twice: distinct (map fst P)
- Every class declaration $(\boldsymbol{C},\,\boldsymbol{D},\,\boldsymbol{f}$ s, m s $)\in$ set \boldsymbol{P} is well-formed.

Well-formed class declaration (**C**, **D**, **fs**, **ms**)

- All field declarations in fs are well-formed
- No field in *fs* is declared twice
- All method declarations in ms are well-formed
- No method in ms is declared twice
- If $C\neq \textit{Object}$ then
	- D is a class in P
	- D is not a subclass of C: \neg $P \vdash D \preceq^* C$
	- Overriding: if $(M, Ts, T, mb) \in set ms$ and $P \vdash D$ sees M: Ts' \rightarrow T' $=$ mb' in D' then $P \vdash \mathcal{T} \leq \mathcal{T}'$ and $P \vdash \mathcal{T}$ s' $[\leq]$ \mathcal{T} s Method overriding is *covariant* in the result type and contravariant in the argument types

Well-formed method declaration (**M**, **Ts**, **T**, **Vs**, **^e**)

- All parameter types are valid: \forall T∈set Ts. is-type P T
- The result type is valid: *is-type P T*
- There are as many parameter types as names: $|T$ s $|=$ $|V$ s $|$
- All parameter names are distinct: *distinct Vs*
- *this* is not a parameter name: *this* \notin set Vs
- The method body is well-typed: \exists $\mathsf{T}'.$ $\mathsf{P},$ [this \mapsto Class C, Vs $[\mapsto]$ Ts] \vdash $\mathsf{e} ::$ $\mathsf{T}' \wedge$ $\mathsf{P} \vdash \mathsf{T}' \leq \mathsf{T}$
- All local variables are assigned to before use: \mathcal{D} e $(\{ \textit{this} \} \cup \textit{set Vs})$

Well-formed field declaration (**F**, **T**)

The type is valid: *is-type P T*